| Tsuyama College | Year | 2021 | Course <br> Title | Differential and Integral II |
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## Course Information

| Course Code | 0058 | Course Category | General / Compulsory |
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| Class Format | Lecture | Credits | School Credit: 2 |
| Department | Department of Integrated Science and <br> Technology Communication and <br> Informations System Program | Student Grade | 3rd |
| Term | Year-round | Classes per Week | 2 |
| Textbook and/or <br> Teaching Materials | Textbook: "Shin bibunsekibun II" (Dainippontosyo) |  |  |
| Instructor | YAMANAKA Satoshi |  |  |

## Course Objectives

## Learning purpose :

By studying the series and the differentiation and integration of two-variable functions, you will acquire the mathematical knowledge and calculation techniques necessary to solve basic engineering problems.

Course Objectives :

1. To expand various functions into power series.
2. To understand the concept of partial differential and be able to obtain the extremal value of two-variable functions and the equation of the tangent plane of surfaces.
3. To understand the concept of double integrals and be able to find the volume of a basic solid.

## Rubric

|  | Excellent | Good | Acceptable | Not acceptable |
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| Achievement 1 | The student can find the McLaughlin expansion of functions. | The student can find the linear and quadratic approximations of the basic function. In addition, be can find the McLaughlin expansion of basic functions. | The student can find the linear and quadratic approximations of the basic function. | The student can not find the linear and quadratic approximations of the basic function. |
| Achievement 2 | The student can find the extremal value of various functions. In addition, can find the conditional extremal value and the envelope. | The student can find the extremal value of basic functions. In addition, can find the envelope. | The student can find the extremal value of basic functions. | The student can not find the extremal value of basic functions. |
| Achievement 3 | The student can calculate double integrals, and can exchange the integral order. | The student can understand the repeated integral, and can find the double integral of basic functions using it. | The student can find the double integral of basic functions by using the iterated integral. | The student can not find the double integral of basic functions by using the iterated integral. |
| Achievement 4 | The student can calculate double integrals by applying change of variables using Jacobian. | The student can calculate double integrals using the conversion from rectangular to polar coordinates. In addition, understand the meaning of polar transformation. | The student can calculate the double integral by using the polar transformation. | The student can not calculate the double integral by using the polar transformation. |

## Assigned Department Objectives

Teaching Method

|  | General or Specialized : General <br> Field of learning : natural science, common and basics <br> Foundational academic disciplines : <br> Mathematical science / mathematics / Basic analysis <br> Relationship with Educational Objectives : <br> This class is equivalent to "(2) Acquire basic science and technical knowledge". <br> Relationship with JABEE programs: <br> The main goal of learning / education in this class are "(A), and A-1". <br> Course outline : <br> Start by understanding the concept of series and the power series expansion of functions. Next, we will <br> develop the differentiation and integration of one-variable functions learned in the second grade, and learn <br> about the differentiation of two-variable functions (partial differentiation) and the integration of two-variable <br> functions (double-integral). |
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|  | Course method : <br> Classes centered on board writing, and emphasize intuitive understanding of content without being biased <br> toward rigor as much as possible. In addition, a lot of exercise time will be provided to deepen the <br> understanding. |
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|  | Precautions on the enrollment : <br> Students must take this class (no more than one-third of the required number of class hours missed) in order <br> to complete the 3rd year course. <br> Course advice : <br> Classes will be conducted while reviewing, but review mathematics (especially differentiation and integration) <br> up to the 2nd year each time. <br> Foundational subjects : <br> Fundamental Mathematics (1st year), Fundamental Mathematics Practice (1st), Differential and Integral I <br> (2nd), Fundamental Linear Algebra (2nd) <br> Related subjects : <br> Applied Mathematics I and II (4th year) <br> Attendance advice : <br> It is important to understand the content of the lecture well and solve the problem by yourself. It is important <br> for students to find solutions on their own. If you are significantly late for class, treat it as absent. If you are <br> late a lot, you may be treated as absent after giving a warning. |
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## Characteristics of Class / Division in Learning

| $\square$ Active Learning | $\square$ Aided by ICT | $\square$ Applicable to Remote Class | $\square$ <br> Experienced |
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## Must complete subjects

## Course Plan

|  |  |  | Theme | Goals |
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| 1st Semeste r | $\begin{array}{\|l\|} \hline \text { 1st } \\ \text { Quarter } \end{array}$ | 1st | Guidance, Polynomial approximation (1) | Students can find the linear approximation and the quadratic approximation of functions. |
|  |  | 2nd | Polynomial approximation (2) | Students can find the $n$-th approximation of functions, and can determine the extremal value of functions. |
|  |  | 3rd | Limit of sequences | Students can find the limit of various sequences including indeterminate forms. |
|  |  | 4th | Series | Students can judge the convergence and the divergence of a series. |
|  |  | 5th | Power series and McLaughlin expansion | Students can find the McLaughlin expansion of a function. |
|  |  | 6th | Euler's formula | Students can calculate complex numbers using Euler's formula. |
|  |  | 7th | Function of two variables | Students can draw a graph of a simple twovariable function. |
|  |  | 8th | 1st semester mid-term exam |  |
|  | 2nd Quarter | 9th | Return and commentary of exam answers, partial derivative | Students can find the partial derivative of twovariable functions. |
|  |  | 10th | Total differential and tangent plane | Students can find the tangent plane equation |
|  |  | 11th | Differential calculus of composite function | Students can find the partial derivative using the derivative of the composite function. |
|  |  | 12th | Higher-order partial derivative | Students can find the higher derivative. |
|  |  | 13th | Maximal value and minimal value | Studentscan find maximal values and minimal values of two-variable functions. |
|  |  | 14th | Exercise |  |
|  |  | 15th | 1st semester final exam |  |
|  |  | 16th | Return and commentary of exam answers |  |
| 2nd Semeste r | 3rd Quarter | 1st | Guidance, Differential of implicit function | Students can find the derivative using the differential of implicit function. |
|  |  | 2nd | Conditional extremum problem | Students can find conditional extrema. |
|  |  | 3rd | Envelope | Students can find the envelope equation. |
|  |  | 4th | Definition of double integral | Students can understand the definition of double integrals, and can express the volume of solids using double integrals. |
|  |  | 5th | Calculation of double integral (1) | Students can calculate the repeated integral. |
|  |  | 6th | Calculation of double integral (2) | Students can calculate the volume of solids using the change of integration order. |
|  |  | 7th | Exercise |  |
|  |  | 8th | 2nd semester mid-term exam |  |
|  | 4th Quarter | 9th | Return and commentary of exam answers, Multiple integral in polar coordinates | Studentscan find the double integral by converting it to polar coordinates. |
|  |  | 10th | Change of variables and multiple integrals | Students can calculate the double integral using the general change of variables. |
|  |  | 11th | Improper integral | Students can calculate the improper integral. |
|  |  | 12th | Various applications of double integrals (1) | Students can find the area of the curved surface. |
|  |  | 13th | Various applications of double integrals (2) | Students can find the barycenter of the figure. |
|  |  | 14th | Exercise |  |
|  |  | 15th | 2nd semester final exam |  |
|  |  | 16th | Return and commentary of exam answers |  |
| Evaluation Method and Weight (\%) |  |  |  |  |


|  | Examination | Presentation | Mutual <br> Evaluations <br> between <br> students | Behavior | Portfolio | Other | Total |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Subtotal | 60 | 0 | 0 | 0 | 0 | 40 | 100 |
| Basic <br> Proficiency | 60 | 0 | 0 | 0 | 0 | 40 | 100 |
| Specialized <br> Proficiency | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| Cross Area <br> Proficiency | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

